

# Package ‘pheno’

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**Title** Auxiliary Functions for Phenological Data Analysis

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**Description** Provides some easy-to-use functions for time series analyses of (plant-) phenological data sets. These functions mainly deal with the estimation of combined phenological time series and are usually wrappers for functions that are already implemented in other R packages adapted to the special structure of phenological data and the needs of phenologists. Some date conversion functions to handle Julian dates are also provided.

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connectedSets	<i>Connected sets in a matrix</i>
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---

## Description

Finds connected data sets, i.e. connected rows and columns of a numeric matrix M.

## Usage

```
connectedSets(M)
```

## Arguments

M                      Numeric matrix with missing values assumed to be NA or 0.

## Details

In a two-way classification of linear models sometimes independent sets of normal equations are obtained due to missing data in the experiments design, i.e. the complete design matrix is not of full rank and thus no solution can be found. However, solutions of the independent sets of normal equations can still exist. This phenomenon is called 'connectedness' of the data. Especially in phenological analysis experimental designs are almost always unbalanced because of missing data. Thus, when combined time series are to be estimated, it is worth checking for and finding connected data sets for which combined time series can then be estimated. Example (also see example data(Simple) and example in 'maxConnectedSet'): In the following matrix dots represent missing values, X represent observations and the lines join the connected sets:

```
: X \ _ _ X . .
: |
: X \ _ _ X . .
:
: . . X \ _ _ X
```

Thus, in this matrix observations in rows 1 and 2 or columns 1 and 2 form one connected set. Likewise row 3 (or columns 3 and 4) form also one connected set.

**Value**

rowclasses	Vector of set numbers of rows of M ( $\geq 1$ ). A value of -1 indicates a row with missing data.
colclasses	Vector of set numbers of columns of M ( $\geq 1$ ). A value of -1 indicates a column with missing data.

**Author(s)**

Joerg Schaber

**References**

Searle (1997) 'Linear Models'. Wiley. page 318.

**See Also**

[maxConnectedSet](#) [getConnectionedSets](#)

**Examples**

```
data(Simple)
connectedSets(Simple)
```

---

date2jul1	<i>Converts string date to Julian date</i>
-----------	--

---

**Description**

Converts a string date "DD.MM.YYYY" into a Julian day of year (DOY).

**Usage**

```
date2jul1(d)
```

**Arguments**

d Date as character string 'DD.MM.YYYY'.

**Value**

doy Day of year as integer.  
year Year as integer.

**Author(s)**

Joerg Schaber

**Examples**

```
date2jul1('31.05.1970')
```

---

date2jul2	<i>Converts a date (day,month,year) to Julian date</i>
-----------	--

---

**Description**

Converts an integer date (day,month,year) into a Julian day of year (DOY). If y is missing, 2000 is assumed.

**Usage**

```
date2jul2(d,m,y)
```

**Arguments**

d	Day of month, numeric coerced into an integer.
m	Month of year, numeric coerced into an integer.
y	Year, numeric coerced into an integer, default 2000.

**Value**

doy	Day of year as integer.
year	Year as integer.

**Author(s)**

Joerg Schaber

**Examples**

```
date2jul2(31,5,1970)
```

---

daylength	<i>Daylength at julian day i on latitude l</i>
-----------	--

---

**Description**

Calculates daylength [h] and declination angle delta [radians] on day i [julian day of year] for latitude l [degrees].

**Usage**

```
daylength(i,l)
```

**Arguments**

i	Integer as julian day of year (1-365)
l	Float as latitude [degress]

**Value**

d1	daylength [h]
delta	declination angle [degrees]

**Author(s)**

Joerg Schaber

**Examples**

```
daylength(as.integer(120),63)
```

---

daysbetween	<i>Number of days between two dates</i>
-------------	---

---

**Description**

Number of days between date1 and date2.

**Usage**

```
daysbetween(d1,d2)
```

**Arguments**

d1	Date as a character string 'DD.MM.YYYY'.
d2	Date as s character string 'DD.MM.YYYY'.

**Value**

ndays                    Number of days between d1 and d2.

**Author(s)**

Joerg Schaber

**Examples**

```
daysbetween('31.05.1970','10.03.2004')
```

---

DWD

*Phenological observations*

---

**Description**

Phenological observations of nine stations from 1951 to 1998. Data from the German Weather Service.

**Usage**

```
data(DWD)
```

**Format**

Data frame containing three columns (day of year of observations,year,station-id)

**Source**

German Weather Service

**References**

Schaber J, Badeck F-W (2002) 'Evaluation of methods for the combination of phenological time series and outlier detection'. *Tree Physiology* 22:973-982

---

getConnectedSets      *Finds connected sets in a matrix or data frame*

---

### Description

Finds a list of connected data sets in a matrix or data frame and returns them accordingly.

### Usage

```
getConnectedSets(M)
```

### Arguments

M                      Numeric matrix with missing values considered as 0, or a data frame. The data frame is internally converted to a matrix and should have three columns (x, factor 1, factor 2) where x are considered the entries of the matrix, rows correspond to levels of factor 2 and columns correspond to levels of factor 1.

### Details

getConnectedSets returns a list of connected data sets as numeric data frames D with three columns (x, factor 1, factor 2) or a n\*m matrix M, where the n rows correspond to n levels of factor 2 and m columns correspond to m levels of factor the respective factors. Output as data frame or matrix, depending on input.

### Value

cs\_i                    List of connected sets as matrix or data frame, corresponding to the input. named as cs\_i with i being the number of the connected sets.

### Author(s)

Joerg Schaber

### References

Searle (1997) 'Linear Models'. Wiley. page 318.

### See Also

[connectedSets](#) [maxConnectedSet](#)

### Examples

```
data(Searle)
getConnectedSets(Searle)
```

---

jul2date1	<i>Converts Julian date into string date</i>
-----------	--

---

**Description**

Converts Julian day of year (DOY) into a string date 'DD.MM.YYYY'. If y is missing a non-leap year is assumed.

**Usage**

```
jul2date1(d,y)
```

**Arguments**

d	DOY, numeric coerced into an integer.
y	Year, numeric coerced into an integer, default 2000.

**Value**

date	Date, as character string 'DD.MM.YYYY'
------	--

**Author(s)**

Joerg Schaber

**Examples**

```
jul2date1(151,1970)
```

---

jul2date2	<i>Converts Julian date to integers day,month,year</i>
-----------	--

---

**Description**

Converts Julian day of year (DOY) into an integer date (day,month,year). If y is missing a non-leap year is assumed.

**Usage**

```
jul2date2(d,y)
```

**Arguments**

d	DOY, numeric coerced into an integer.
y	Year, numeric coerced into an integer, default 2000.



**Value**

day	Day of month as integer.
month	Month of year as integer.
year	Year as integer.

**Author(s)**

Joerg Schaber

**Examples**

```
jul2date2(151,1970)
```

---

leapyear	<i>Boolean test for leap year</i>
----------	-----------------------------------

---

**Description**

Tests whether a given year is a leap year or not.

**Usage**

```
leapyear(y)
```

**Arguments**

y	Year, numeric coerced into integer.
---	-------------------------------------

**Value**

TRUE	leap year
FALSE	non leap year

**Author(s)**

Joerg Schaber

**Examples**

```
leapyear(2000)  
leapyear(2004)
```

---

matrix2raw	<i>Converts numeric matrix to data frame</i>
------------	--

---

### Description

Converts a numeric matrix *M* into a dataframe *D* with three columns (*x*, factor 1, factor 2) where rows of *M* are ranks of factor 1 levels and columns of *M* are ranks of factor 2 levels, missing values are assumed to be 0 or NA. The resulting dataframe *D* has no missing values.

### Usage

```
matrix2raw(M,l1,l2)
```

### Arguments

<i>M</i>	Numeric matrix, with missing values assumed to be NA or 0.
<i>l1</i>	<b>Optional</b> numeric vector of level names of column 2 (factor 1) of returned data frame. If missing it is assigned row numbers of <i>M</i> .
<i>l2</i>	<b>Optional</b> numeric vector of level names of column 3 (factor 2) of returned data frame. If missing it is assigned column numbers of <i>M</i> .

### Value

<i>D</i>	Data frame with three columns: ( <i>y</i> , <i>f1</i> , <i>f1</i> ). <i>y</i> : observations, i.e. non-zero entries, in matrix. <i>f1</i> : factor 1, i.e. row number of <i>M</i> or <i>l1</i> . <i>f2</i> : factor 2, i.e. column number of <i>M</i> or <i>l2</i> . <i>D</i> is ordered first by factor 2 and then factor 1. <i>D</i> has no missing values.
----------	---

### Author(s)

Joerg Schaber

### Examples

```
data(DWD)
M <- raw2matrix(DWD) # conversion to matrix
D1 <- matrix2raw(M) # back conversion, but with different level names
D2 <- matrix2raw(M,c(1951:1998),c(1:9)) # with original level names
```

---

maxConnectedSet	<i>Maximal connected set in a matrix</i>
-----------------	--

---

## Description

Finds connected data set, i.e. connected rows and columns of a numeric matrix  $M$ , that has the largest number of data entries.

## Usage

```
maxConnectedSet(M)
```

## Arguments

$M$	Numeric matrix with missing values considered as 0, or a data frame. The data frame is internally converted to a matrix and should have three columns (x, factor 1, factor 2) where x are considered the entries of the matrix, rows correspond to levels of factor 2 and columns correspond to levels of factor 1.
-----	---

## Details

In a two-way classification of linear models sometimes independent sets of normal equations are obtained due to missing data in the experiments design, i.e. the complete design matrix is not of full rank and thus no solution can be found. However, solutions of the independent sets of normal equations can still exist. This phenomenon is called 'connectedness' of the data. Especially in phenological analysis experimental designs are almost always unbalanced because of missing data. Thus, when combined time series are to be estimated, it is worth checking for and finding connected data sets for which combined time series can then be estimated. This can also be interpreted in the way that a prerequisite to obtain a combined time series is to have overlapping time series. Example (also see example data(Searle) from Searle (1997), page 324 and example in 'connectedSets'): In the following matrix dots represent missing values, X represent observations and the lines join the connected sets:

```
: X \ \ \ . \ \ \ . \ \ \ . \ \ \ X . . .
: |
: . . X \ \ \ . \ \ \ ! \ \ \ . \ \ \ . \ \ \ X
: | |
: . X \ \ \ . \ \ \ . \ \ \ ! \ \ \ X \ \ \ X !
: | | |
: . X \ \ \ . \ \ \ . \ \ \ ! \ \ \ X \ \ \ X !
: | |
: . . . . X . . !
: | |
: . . X \ \ \ . \ \ \ ! \ \ \ . \ \ \ . \ \ \ X
: |
: . . . X \ \ \ X . . .
```

Thus, in this matrix observations of rows 1, 5 and 7 or columns 1, 4 and 5 form one connected set. Likewise observations of rows 2 and 6 (or columns 3 and 8) and rows 3 and 4 (or columns 2, 6 and 7) form also connected sets, respectively.

### Value

ms	maximal connected set as matrix or data frame, corresponding to the input.
maxl	Number of observations in the maximal connected data set.
nsets	Number of connected data sets.
lsets	Vector with number of observations in each connected data sets, i.e. lsets[i] is the number of observations in connected data set i.

### Author(s)

Joerg Schaber

### References

Searle (1997) 'Linear Models'. Wiley. page 318.

### See Also

[connectedSets](#) [maxConnectedSet](#)

### Examples

```
data(Searle)
maxConnectedSet(Searle)
```

---

maxdaylength	<i>Maximal day length on latitude l</i>
--------------	---

---

### Description

Calculates maximal daylength maxdl [h] at a certain latitude l [degrees].

### Usage

```
maxdaylength(l)
```

### Arguments

l	Latitude in degrees.
---	----------------------

### Value

maxdl	Maximal daylength [h] at a certain latitude l [degrees]
-------	---

**Author(s)**

Joerg Schaber

**Examples**

```
maxdaylength(60)
```

---

 pheno.ddm

*Dense design matrix for phenological data*


---

**Description**

Creation of dense two-way classification design matrix. The sum of the second factor is constrained to be zero. No general mean.

**Usage**

```
pheno.ddm(D, na.omit=TRUE)
```

**Arguments**

D	Data frame with three columns: (observations, factor 1, factor 2).
na.omit	Determined whether missing values should be omitted or not. Default is TRUE.

**Details**

In phenological applications observations should be the julian day of observation of a certain phase, factor 1 should be the observation year and factor 2 should be a station-id. Usually this is much easier created by: `y <- factor(f1), s <- factor(f2), ddm <- as.matrix.csr(model.matrix(~ y + s - 1, contrasts=list(s="contr.sum")))`. However, this procedure can be quite memory demanding and might exceed storage capacity for large problems. This procedure here is much less memory consuming. Moreover, in order to get direct estimates for all coefficients, an additional row is appended to the matrix, where the columns for the second factor are set to 1. Therefore, dimensions of ddm are  $(nlevels(factor1)+1) \times (nlevels(factor2))$ .

**Value**

ddm	Dense roworder matrix, matrix.csr format (see matrix.csr in package SparseM)
D	Data frame D sorted first by f2 then by f1 and with rows containing NA's removed.
na.rows	Rows in D that were omitted due to missing values.

**Author(s)**

Joerg Schaber

**See Also**[model.matrix matrix.csr](#)**Examples**

```
data(DWD)
ddm1 <- pheno.ddm(DWD)
attach(DWD)
y <- factor(DWD[[2]])
s <- factor(DWD[[3]])
ddm2 <- as.matrix.csr(model.matrix(~ y + s -1, contrasts=list(s=("contr.sum"))))
identical(ddm1$ddm, ddm2)
```

---

`pheno.flm.fit`*Fits a two-way linear fixed model*

---

**Description**

Fits a two-way linear fixed model. The model assumes the first factor f1 the second factor f2 to be fixed. Errors are assumed to be i.i.d. No general mean and sum of f2 is constrained to be zero.

**Usage**

```
pheno.flm.fit(D, limit=1000)
```

**Arguments**

<code>D</code>	Data frame with three columns (x, f1, f2) or a matrix where rows are ranks of factor f1 levels and columns are ranks of factor f2 levels and missing values are assumed to be NA or 0.
<code>limit</code>	Integer that determines which algorithm to use (see Details).

**Details**

This function is basically a wrapper for the `s1m.fit()` function from the `SparseM` package, adapted for the estimation of combined phenological time series. In phenological application, `x` should be the julian day of observation of a certain phase, factor `f1` should be the observation year and factor `f2` should be a station-id. For large problems `length(x) > limit`, the linear model is calculated for treatment contrasts for efficiency reasons, and the constraint that the sum of `f2` is zero, is adjusted afterwards. This results in a slight over-estimation of standard errors. Note that the input data is sorted before fitting, such that subsequent analyses using the input data should be done using the sorted output data frame.

**Value**

f1	Estimated fixed effects f1, in phenology this is precisely the combined time series.
f1.se	f1 estimated standard error.
f1.lev	Levels of f1. Should be the same order as f1.
f2	Estimated fixed effects f2, in phenology these are the station effects.
f2.se	f2 estimated standard error.
f2.lev	Levels of f2. Should be the same order as f2.
resid	Residuals
lclf1	Lower 95 percent confidence limit of factor f1.
uclf1	Upper 95 percent confidence limit of factor f1.
lclf2	Lower 95 percent confidence limit of factor f2.
uclf2	Upper 95 percent confidence limit of factor f2.
D	The input as ordered data frame, ordered first by f2 then by f1
fit	The fitted lm model object.

**Author(s)**

Joerg Schaber

**References**

Searle (1997) 'Linear Models'. Wiley. Schaber J, Badeck F-W (2002) 'Evaluation of methods for the combination of phenological time series and outlier detection'. *Tree Physiology* 22:973-982

**See Also**

[lm](#)

**Examples**

```
data(DWD)
R <- pheno.flm.fit(DWD) # parameter estimation
```

---

pheno.lad.fit

*Fits a robust two-way linear model*

---

**Description**

Fits a robust two-way linear model. The model assumes both factors (f1 and f2) to be fixed. Errors are assumed to be i.i.d. No general mean and sum of f2 is constrained to be zero.

**Usage**

```
pheno.lad.fit(D, limit=1000)
```

**Arguments**

<code>D</code>	Data frame with three columns ( <code>x</code> , <code>f1</code> , <code>f2</code> ) or a matrix where rows are ranks of factor <code>f1</code> levels and columns are ranks of factor <code>f2</code> levels and missing values are assumed to be <code>NA</code> or <code>0</code> .
<code>limit</code>	Integer that determines which algorithm to use (see Details).

**Details**

The function minimizes the least absolute deviations (LAD or L1 norm) of the residuals of a two-way linear model. This function is basically a wrapper for the `rq.fit()` or `rq.fit.sfn()` functions of the `quantreg` package, respectively, adapted for the estimation of combined phenological time series. Depending on the size of the problem `length(x) <= limit` either the `rq.fit()` function using the Barrodale-Roberts algorithm is used or (`length(x) > 1000`) the corresponding dense matrix implementation with `rq.fit.sfn()` using the Interior-Point method. In phenological applications, `x` should be the julian day of observation of a certain phase, factor `f1` should be the observation year and factor `f2` should be a station-id. For efficiency reasons, the linear model is calculated for treatment contrasts and the constraint that the sum of `f2` is zero, is adjusted afterwards. Note that the input data is sorted before fitting, such that subsequent analyses using the input data should be done using the sorted output data frame.

**Value**

<code>f1</code>	Estimated parameters of factor <code>f1</code> , in phenology this is precisely the combined time series.
<code>f1.lev</code>	Levels of <code>f1</code> . Should be the same order as <code>f1</code> .
<code>f2</code>	Estimated parameters of factor <code>f2</code> , in phenology these are precisely the station effects.
<code>f2.lev</code>	Levels of <code>f2</code> . Should be the same order as <code>f2</code> .
<code>resid</code>	Residuals
<code>ierr</code>	For <code>length(x) &gt; 1000</code> this is the return error code of <code>rq.fit.sfn()</code>
<code>D</code>	The input as ordered data frame, ordered first by <code>f2</code> then by <code>f1</code>
<code>fit</code>	The fitted <code>rq.fit</code> model object.

**Author(s)**

Joerg Schaber

**References**

Rousseeuw PJ, Leroy AM (1987) 'Robust estimation and outlier detection'. Wiley. Schaber J, Badeck F-W (2002) 'Evaluation of methods for the combination of phenological time series and outlier detection'. *Tree Physiology* 22:973-982



**See Also**

[rq.fit](#) [rq.fit.sfn](#)

**Examples**

```
data(DWD)
R <- pheno.lad.fit(DWD) # robust parameter estimation
plot(levels(factor(R$D[[2]])),R$p1,type="l") # plot combined time series
R$D[R$resid >= 30,] # observation whose residuals
# are > 30 days (outliers)
```

---

pheno.mlm.fit	<i>Fits a two-way linear mixed model</i>
---------------	--

---

**Description**

Fits a two-way linear mixed model. The model assumes the first factor f1 to be fixed and the second factor f2 to be random. Errors are assumed to be i.i.d. No general mean and sum of f2 is constrained to be zero.

**Usage**

```
pheno.mlm.fit(D)
```

**Arguments**

D	Data frame with three columns (x, f1, f2) or a matrix where rows are ranks of factor f1 levels and columns are ranks of factor f2 levels and missing values are set to 0.
---	---

**Details**

This function is basically a wrapper for the `lme()` function of the `nlme` package, adapted for the estimation of combined phenological time series. Estimation method: restricted maximum likelihood (REML) In phenological application, x should be the julian day of observation of a certain phase, factor f1 should be the observation year and factor f2 should be a station-id. Note that the input data is sorted before fitting, such that subsequent analyses using the input data should be done using the sorted output data frame.

**Value**

fixed	Estimated fixed effects, in phenology this is precisely the combined time series.
fixed.lev	Levels of fixed effects. Should be the same order as fixed effects.
random	Estimated random effects, in phenology these are the station effects.
random.lev	Levels of random effects. Should be the same order as random effects.
SEf1	Standard error group f1, i.e. square root of variance component fixed effect.

SEf2	Standard error group f2, i.e. square root of variance component random effect.
lclf	Lower 95 percent confidence limit of fixed effects.
uclf	Upper 95 percent confidence limit of fixed effects.
D	The input as ordered data frame, ordered first by f2 then by f1
fit	The fitted lme model object.

**Author(s)**

Joerg Schaber

**References**

Searle (1997) 'Linear Models'. Wiley. Schaber J, Badeck F-W (2002) 'Evaluation of methods for the combination of phenological time series and outlier detection'. Tree Physiology 22:973-982

**See Also**

[lme](#)

**Examples**

```
data(DWD)
R <- pheno.nlm.fit(DWD) # parameter estimation
plot(levels(factor(DWD[[2]])),R$fixed,type="l") # plot combined time series
tr <- lm(R$fixed~rank(levels(factor(DWD[[2]]))))# trend estimation
summary(tr)$coef[2] # slope of trend
summary(tr)$coef[4] # standard error of trend
```

---

raw2matrix

*Converts a numeric data frame to matrix*


---

**Description**

Converts a numeric data frame D with three columns (x, factor 1, factor 2) to a numeric matrix M where rows are ranks of levels of factor 1 and columns are ranks of levels of factor 2, missing values are set to NA.

**Usage**

```
raw2matrix(D)
```

**Arguments**

D Data frame with three columns (x, factor 1, factor 2)

**Value**

M Numeric matrix where rows are ranks of levels of factor 1 and columns are ranks of levels of factor 2, missing values are set to NA.

**Author(s)**

Joerg Schaber

**Examples**

```
data(DWD)
raw2matrix(DWD)
```

---

Searle

*Example of a two-way classification table*

---

**Description**

Example of a two-way classification table where lacking data creates three distinct connected sets.

**Usage**

```
data(Searle)
```

**Format**

R source file

**References**

Searle (1997) 'Linear Models'. Wiley. 324p.

---

seqMK

*Sequential Mann-Kendall test for time series.*

---

**Description**

The sequential Mann-Kendall test on time series  $x$  detects approximate potential trend turning points in time series.

**Usage**

```
seqMK(x)
```

**Arguments**

$x$  Numeric vector  $x$ .

**Details**

Implicitly assumes a equidistant time series  $x$ . Calculates a progressive and a retrograde series of Kendall normalized tau's. Points where the two lines cross are considered as approximate potential trend turning points. When either the progressive or retrograde row exceed certain confidence limits before and after the crossing points, this trend turning point is considered significant at the corresponding level, i.e. 1.96 for 95

**Value**

prog	Progressive row of Kendall's normalized tau's
retr	Retrograde row of Kendall's normalized tau's
tp	Boolean vector indicating at what indices of the original timeseries the prog and retr cross, i.e. TRUE at potential trend turning points.

**Author(s)**

Joerg Schaber

**References**

Kendall M, Gibbons JD (1990) 'Rank correlation methods'. Arnold. Sneyers R (1990) 'On statistical analysis of series of observations. Technical Note No 143. Geneva. Switzerland. World Meteorological Society. Schaber J (2003) 'Phenology in German in the 20th Century: Methods, analyses and models. Ph.D. Thesis. University of Potsdam. Germany. <https://nbn-resolving.org/urn:nbn:de:kobv:517-0000532>

---

Simple

*Simple example of a two-way classification table*

---

**Description**

Simple example of a two-way classification table where missing data creates two distinct connected sets.

**Usage**

```
data(Simple)
```

**Format**

R source file

---

tau	<i>Kendall's normalized tau</i>
-----	---------------------------------

---

**Description**

Kendall's normalized tau for time series x

**Usage**

tau(x)

**Arguments**

x                      Numeric vector x.

**Details**

Implicitly assumes a equidistant time series x.

**Value**

t                      Kendall's normalized tau.

**Author(s)**

Joerg Schaber

**References**

Kendall M, Gibbons JD (1990) 'Rank correlation methods'. Arnold. Sneyers R (1990) 'On statistical analysis of series of observations. Technical Note No 143. Geneva. Switzerland. World Meteorological Society. Schaber J (2003) 'Phenology in German in the 20th Century: Methods, analyses and models. Ph.D. Thesis. University of Potsdam. Germany. <https://nbn-resolving.org/urn:nbn:de:kobv:517-0000532>

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